

## ALGEBRA 2

### Systems of equations in three unknowns.

Solve the following systems of equations.

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|------------------------|------------------|--------------------|
| $x + 2y - z = 9$       | $x + y + z = 6$  | $x + y + z = 2$    |
| $2x - z = -2$          | $2x - y + z = 3$ | $-x + 3y + 2z = 8$ |
| 1. $3x + 5y + 2z = 22$ | 2. $3x - z = 0$  | 3. $4x + y = 4$    |
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|---------------------|------------------|-------------------|
| $4x + y - 3z = 11$  | $2x + 2z = 2$    | $6y + 4z = -12$   |
| $2x - 3y + 2z = 9$  | $5x + 3y = 4$    | $3x + 3y = 9$     |
| 4. $x + y + z = -3$ | 5. $3y - 4z = 4$ | 6. $2x - 3z = 10$ |
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|----------------------|-----------------------|-----------------------|
| $2x + 4y + z = -4$   | $3x - 2y + 4z = 1$    | $5x - 3y + 2z = 3$    |
| $2x - 4y + 6z = 13$  | $x + y - 2z = 3$      | $2x + 4y - z = 7$     |
| 7. $4x - 2y + z = 6$ | 8. $2x - 3y + 6z = 8$ | 9. $x - 11y + 4z = 3$ |
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|-------------------------|-------------------------|---------------------------|
| $3x + 3y + 5z = 1$      | $2x + y + 3z = 1$       | $x + 2y - 7z = -4$        |
| $3x + 5y + 9z = 0$      | $2x + 6y + 8z = 3$      | $2x + y + z = 13$         |
| 10. $5x + 9y + 17z = 0$ | 11. $6x + 8y + 18z = 5$ | 12. $3x + 9y - 36z = -33$ |
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|---------------------------|-------------------------|------------------------|
| $2x + y - 3z = 4$         | $4x - y + 5z = 11$      | $x - 2y + 5z = 2$      |
| $4x + 2z = 10$            | $x + 2y - z = 5$        |                        |
| 13. $-2x + 3y - 13z = -8$ | 14. $5x - 8y + 13z = 7$ | 15. $3x + 2y - z = -2$ |

### Answers

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|------------|------------|-------------|-------------|------------|
| $x = -1$   | $x = 1$    | $x = 0$     | $x = 2$     | $x = -4$   |
| $y = 5$    | $y = 2$    | $y = 4$     | $y = -3$    | $y = 8$    |
| 1. $z = 0$ | 2. $z = 3$ | 3. $z = -2$ | 4. $z = -2$ | 5. $z = 5$ |
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- |            |            |                |
|------------|------------|----------------|
| $x = 5$    | $x = 1/2$  | $x = 1$        |
| $y = -2$   | $y = -3/2$ | $y = -3/2$     |
| 6. $z = 0$ | 7. $z = 1$ | 8. No solution |
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- |         |            |                |               |
|---------|------------|----------------|---------------|
| $x = 1$ | $y = -3/2$ | 9. No solution | 10. $z = 1/2$ |
|---------|------------|----------------|---------------|

$$\begin{array}{lll} x = 3/10 & x = 5/3 & \\ y = 2/5 & y = 17/3 & x = -z \\ \text{11. } z = 0 & \text{12. Infinite solutions} & \text{13. } z = 5/3 \\ & & \text{14. Infinite solutions} & \text{15. } y = 2z - 1 \end{array}$$